

# Supplementary Material

## 1 Details of CNN Structures

The AlexNet [14] based image CNN we use in the experiments is structured as follows:

conv $11 \times 11 \times 96$ , stride 2, valid padding maxpool size 4, stride 2
conv $5 \times 5 \times 192$ maxpool size 4, stride 2
conv $3 \times 3 \times 384$ conv $3 \times 3 \times 256$ conv $3 \times 3 \times 256$ maxpool size 4, stride 2
fc 4000 fc 4000 sigmoid 10

Table 1: Image CNN, standalone

The image CNN takes image input of size  $227 \times 227$ . During training, a raw image is cropped to this size at random positions; during inference, we crop the center patch of images to match the size.

The coefficient CNN can have replaceable convolutional layers. When trained or evaluated separately, the full structure is as follows:

(F-B conv layers)
fc 256 fc 256 sigmoid 10

Table 2: Coefficient CNN, standalone

The joint network is structured as follows:

(Image conv layers)   (F-B conv layers)
concat fc 4000 fc 4000 sigmoid 10

Table 3: Joint network

## 2 Experiments of F-B CNN Architectures

We devise several different network structures to run on Fourier-Bessel coefficients for comparison (listed in Table 4). Because the Fourier-Bessel images are not big (only  $40 \times 11 \times 2$ ), we only investigate up to four convolutional layers. Our principle of probing coefficient network structures is to imitate the design of VGGNet [22], which is also the methodology

of He et al.’s experiments of residual networks [7], i.e., we apply homogeneous  $3 \times 3$  convolutions solely and double the number of output maps right after any max-pooling. Each network structure is applied to both raw F-B coefficients and log F-B coefficients via (10).

We run training and testing with these convolutional configurations, and record the mean average precisions (mAPs) of the 10 attributes in Table 5. Experimental results confirm the common belief that more convolutional layers lead to better performance, but specific processing such as max-pooling and pseudo-log is crucial for convergence.

1conv	2conv	3conv	4conv	2c-pool-2c
(3, 64)	(3, 64)	(3, 64)	(3, 64)	(3, 64)
	(3, 128)	(3, 128)	(3, 128)	(3, 128)
				maxpool
		(3, 128)	(3, 128)	(3, 256)
			(3, 128)	(3, 256)

Table 4: Configuration of Experimental Architectures. Conv layers are denoted as (filtersize, #output featmaps), and `maxpool` is a max-pooling layer with window size 4 and stride 2.

Architecture	mAP	
	Raw	Log
1conv	0.7031	0.6860
2conv	0.7305	0.7164
3conv	0.6703	0.7072
4conv	0.6649	0.6420
2c-pool-2c	0.6817	<b>0.7450</b>

Table 5: Mean Average Precision with Different Coefficient CNN Architectures. Raw: Fourier-Bessel coefficients are fed into coefficient CNN with no processing. Log: Pseudo-log (10) is performed.